Impact Analysis on Water Quality of the Second Songhua River Based on Mathematical Model

Sun Shao-Chen, Zhou Zu-Hao, Xiao Wei-Hua, and Wang Hao

Abstract-Water quality of the second Songhua River is affected by both tributary pollution loads and upper boundary. A set of hydrodynamics and water quality coupling model of the second Songhua River was developed. Based on the model, the pollution contribution ratios of tributaries pollution loads and boundaries were ascertained. The impacts of the change of water qualities of upper boundary and tributary were analyzed, and the farthermost water quality improvement of second Songhua River when upper boundary being better and tributary meeting Class III of National Surface Water Quality Standard was predicted. The results indicated: 1)if the tributary (Yinma river)meets Class III of National Surface Water Quality Standard, the water quality of WUJIA water quality monitoring station in Songhua river improving will be bigger from Jun through Aug, Ammonia and Nitrogen Index was significantly improved, but to upper boundary, this kind of impact is bigger. 2) Both reducing the tributaries pollution loads and improving upper boundaries are necessary for improving water quality in the second Songhua River.

Index Terms—Mathematical model, the second Songhua River, tributary, water qualities .

I. INTRODUCTION

The second Songhua River takes an important place in the economic development in Jilin province. However, in recent years many problems have been brought about by irrational reclamation of wasteland, irrational diversion from the source streams and large volume of untreated sewage drained into the river.

From Table I, we can see the water quality deterioration at the downstream of the Long tan Bridge in city of Jilin, especially at the downstream of the Songhua river (VI) monitoring station, the water is seriously polluted and has a trend of becoming more and more seriously. The major pollution indexs was BOD_5 , COD and NH_3 -N.

In 2005, the tributaries in inland river basins including Huifa river, Yinma river and Yitong river have bad water qualities (poor V) [1]. The major pollution indexs was BOD₅, COD and NH₃-N.

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Monitoring sections	2000	2001	2002	2003	2004	2005	major pollution index
White mountain bridge	III	IV	III	III	III	IV	COD _{Mn}
Linjiang bridge	IV	IV	IV	III	III	IV	COD _{Mn}
Fengman	III	III	III	III	III	III	
Longtan bridge	III	III	III	III	III	III	
Nine stage	V	V	V	IV	IV	IV	NH ₃ -N
Shaokou	V	IV	III	IV	IV	IV	NH3-N
Baiqi	IV	IV	III	IV	III	III	COD _{Mn}
Songhua river(six)	IV	III	III	>V	V	>V	COD _{Mn}
Zhenjiangkou	IV	IV	III	>V	>V	V	NH ₃ -N
Stock farm station	IV	IV	III	III	III	III	COD _{Mn}
Hogwash crock	IV	IV	IV	III	III	III	COD _{Mn}

TABLE II: WATER QUALITY STATE OF THE SECOND SONGHUA RIVER

From Table II, Monitoring results indicated that the Dehui station which is a part of Yinma River and Kaoshan station which is a part of Yitong River have worse water quality, which indicates this area has received lots of pollution sources. The water quality of main stream will be influenced when the water of tributaries flow into.

TABLE II: THE WATER QUALITY OF YINMA RIVER AND YITONG RIVER IN 2007

tributaries	water quality station	NH ₃ -N	COD _{cr}	COD_{mn}	BOD ₅
Yinma river	Dehui	IV	V	IV	V
Yitong river	Kaoshan	V	>V	>V	>V

The water quality of the second Songhua River receives much concern all the time [2-7]. The water quality is affected by upriver, local pollution source and the tributaries. The second Songhua River is broad and has a well-developed river system, and each water area in the river basin has different environmental conditions, hydrology conditions and chemical compositions, also the type and quantity of pollution that has been received are different, the pollution conditions are different from parts of the main river to the tributaries. It is necessary to analyze the influence of water quality from upriver and tributaries. This paper studies the influence factors of the second Songhua river pollution using the mathematical model.

Water quality question in water bodies have been extensively studied using various numerical models in the past decades. The implicit finite-difference method has been widely used for the solution of one-dimensional unsteady open-channel flow problems [8-12], Mossman et al. [13] set up one-dimensional unsteady contaminant transport model

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for rivers networks using a split-operator format for solving the advective-dispersive-reactive equation. Vieira [14] developed water quality module CCHE1D-WQ to simulate transport in streams for continuous, unsteady flow by a control volume method.

The aim of this work is to establish a hydrodynamic and water quality model for the second Songhua river networks. This article uses a nonlinear fully-implicit finite difference scheme to discretize the Saint-Venant equations and applies the method of three-step solution for river networks and channel-junction-channel to simulate the river networks.

The simulated water quality constituents concentration, water level and discharge are in good agreement with field observations. The influence of the main river from upriver and tributaries are compared, and the farthermost water quality improvement of the second Songhua river when upper boundary being better and tributary meeting class III of National Surface Water Quality Standard is predicted. Decision-making judgments for govern project of Songhua river are provided.

II. MATHEMATIC MODEL

A. Hydrodynamic Model

1-D Saint-Venant equation set is used to simulate the water flow movement of river network written as follows: Continuity equation:

$$\frac{\partial Q}{\partial s} + B \frac{\partial z}{\partial t} = q_L \tag{1}$$

Momentum equation:

$$\frac{\partial Q}{\partial t} + \frac{\partial}{\partial s} \left(\frac{Q^2}{A} \right) + gA \frac{\partial Z}{\partial s} + g \frac{Q|Q|}{V^2 AR} = 0$$
(2)

in which s denotes the distance in x direction, t is time variable, Q and Z are the section average discharge and water level, g is the acceleration of gravity, B is the total water surface width, q_L is the lateral inflow, R is the hydraulic radius, V is the Chezy coefficient, A is the lateral cross section area.

The governing equations can be discretized with implicit finite-difference method, which has been described concretely in previous studies.

B. Water Quality Model

One-dimensional water quality model written as follows:

$$\frac{\partial C}{\partial t} + u \frac{\partial C}{\partial x} = E \frac{\partial^2 C}{\partial x^2} - kc$$
(3)

where C is the concentration of pollutant constituents, u is the velocity of flow, E is the dispersion coefficient (Fisher Semi-empirical Formula), x is the longitudinal coordinates, t is the time, k is the mass decay rate.

The water quality equation is descretized by the implicit scheme:

$$D_i C_{i-1}^{j+1} + B_i C_i^{j+1} + U_i C_{i+1}^{j+1} = F_i$$
(4)

where D_i , B_i , U_i and F_i are the coefficients of Eq. solving

matrix with pursuing method.

III. CALIBRATION OF HYDRODYNAMIC AND WATER QUALITY MODEL

A. Calibration of Hydrodynamic Model

Fig. 1 shows the structure of study area, where the water quality is poor, and in which the Songhua River (VI) hydrometric station is sited upstream boundary, while the Fuyu (III) hydrometric station is settled downstream boundary. The space step is 500m and the time step is 10min in the simulation. The upstream boundary is given discharge curve and the downstream boundary is preset stage hydrograph in the process of hydrodynamic calculation. Hydrodynamic model is calibrated and verified by measured data of water level and flow from April to October in 2006 and 2007. The roughness coefficient, which is the basic calibration parameter, is $0.025 \sim 0.033$ through calibrating in this area. Some calibration results are shown as Fig. 2 and Fig. 3. The water level and flow of the calculated values and measured values are quite consistent from the calibration verification results. Based on the analysis, we can conclude that the calibrated model could meet the needs of the engineering analysis accuracy.





B. Calibration of Water Quality Model

The time-histories on consistence of ammonia nitrogen and COD variables are given by the water quality boundary. The COD concentration is $10 \sim 15$ mg/l and the ammonia nitrogen concentration is $0.5 \sim 0.7$ mg/l on the serial sections between the main stream way upstream and downstream at the beginning. Meanwhile the COD concentration is $30 \sim$ 50mg/l and the ammonia nitrogen concentration is $3 \sim$ 35mg/l on the section of the tributary. The attenuation coefficient of COD is $0.15 \sim 0.33$ per day and the ammonia nitrogen is $0.08 \sim 0.25$ per day.

The verified results of water quality model which are calibrated with the synchronism hydrology and water quality monitoring data from April to October in 2007 is shown as Fig. 4. The calibrate attenuation coefficient is similar to the value offered by the Songliao Water Conservation Commission. All the calculated relative error of water quality variable density are lower than 20%, except the COD relative error of water quality variable density are closed to 30% at exception moment. This indicated that the model could meet the need of water quality simulation.



Fig. 4. Comparison of constituent concentration at WUJIA water quality monitoring station

IV. IMPACT ANALYSIS ON WATER QUALITY OF THE SECOND SONGHUA RIVER BASED ON MATHEMATICAL MODEL

On the basis of the above study, to study the Impact analysis of upriver and tributaries on water quality of the second Songhua river main stream further, two schemes of simulating are presented: a) assumed that the water quality of tributary is improved from poor V to III of surface water quality standard in the same period, while the water quality of mainstream upstream inflow does not change; Secondly, the pollution load of upstream boundary water is reduced by 10% and its quality of tributaries water does not change. Under the Conditions of assumptions, changes of the water quality of Wujia station are shown as follows:



Fig. 5. Major pollution index concentration at WUJIA station under various conditions

A curve represents the background value (initial value); B curve represents changes in water quality when the tributary water quality reach the standardIII; C curve represents changes in water quality when the upper boundary water quality is improved.

From B curve in Fig. 5 We know that the water quality of downstream improved obviously from Jun to Aug, In the case of the Yinma III level during April to October, the index of NH_3 -N improved better than COD, the maximum rate value of concentration changes will be up to 20%, and there is no significant improvement in other months.

After the analysis of data, the main reasons are: 1) Ammonia nitrogen pollution is serious than COD pollution in the tributaries. 2) As shows in Fig. 6, the ratio of daily average discharges of Dehui to daily average discharges of Songhua river station is bigger during Jun to Aug in 2007, even to 30%. And at this time, the improvements of tributaries water quality have great influence of the main river. Most of the time, the rate is only below 5‰, that means the pollution from Yinma river flows in the main river will be diluted 200 times, so the density of the pollution from Yinma river will be greatly reduced.



Fig. 6. The ratio of daily average discharges of Dehui to daily average discharges of Songhua river station in 2007

Wujia water quality station has a certain degree of improvement according to water simulation results under conditions of two assumptions, in Fig. 5, while which can improve the quality more than major, also need to compare the pollution load reduction ratio of the tributary and upper boundary.

Curve B and C represent water quality changes, which seem approaching. But from the Table III, NH₃-N pollution load of tributary need to cut down more than 90%, CODcr pollution load need to reduce more than 40%, when

tributary(Yinma river)meets Class III of National Surface Water Quality Standard, and river upstream pollution load only reduced by10%. According to the Changes in water quality of Wujia monitoring station in the downstream of the second Songhua river under the two scenarios and the pollution load reduction ratio of the tributary and upper boundary, the proportion of the upper boundary conditions have an absolute advantage in water quality improvement of main stream.

TABLE III: THE RATIO OF POLLUTION LOAD REDUCTION WHEN TRIBUTARY (YINMA RIVER) MEETS CLASS III OF NATIONAL SURFACE WATER QUALITY
STANDADD

Pollution Index	Apr	May	Jun	Jul	Aug	Sep	Oct
NH ₃ -N	94.67%	94.36%	93.84%	94.49%	94.85%	95.02%	88.83%
CODcr	49.84%	56.33%	39.49%	42.10%	45.05%	41.94%	37.11%

V. CONCLUSION

A set of hydrodynamics and water quality model of the second Songhua River is developed. Based on it, the water quality in Yinma River meeting Class III of National Surface Water Quality Standard is predicted. The results indicated: if the tributaries meet Class III of National Surface Water Quality Standard, the water quality of Songhua River improving is bigger from Jun through Aug., ammonia nitrogen index is significantly improved.

Generally speaking, the ratio of daily average discharges of Dehui to daily average discharges of Songhua River (VI) station is only below 5‰, which means the pollution from Yinma river flows in the main river will be diluted 200 times. So the density of the pollution will be greatly reduced which can cause Yinma river water quality doesn't have an obvious effect on the main stream water quality most of the time.

The analysis shows that ammonia nitrogen index of main stream is influenced obviously by Yinma River in high flow period. Through evaluate the influence of Yinma river, analogize other tributaries (flow smaller and water quality better than Yinma river), which is less influence on the water quality of main stream.

According to the Changes in water quality of Wujia monitoring station in the downstream of the second Songhua River under the two scenarios and the pollution load reduction ratio of the tributary and upper boundary, the proportion of the upper boundary conditions have an absolute advantage in water quality improvement of main stream.

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